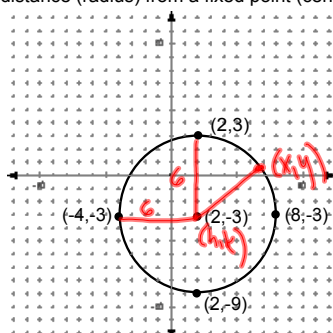


8-3 Circles

Circle—the set of all points, in a plane, a given distance (radius) from a fixed point (center)



$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$r = \sqrt{(x - h)^2 + (y - k)^2}$$

Equation of Circle

$$r^2 = (x - h)^2 + (y - k)^2$$

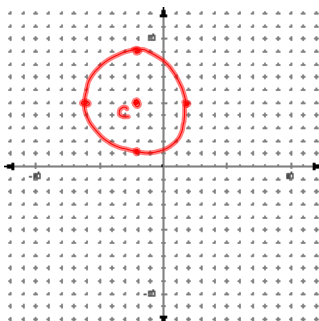
$$C(h, k)$$

Find the equation of a circle with $C(-2, 5)$ and $r = 4$.

$$r^2 = (x - h)^2 + (y - k)^2$$

$$16 = (x + 2)^2 + (y - 5)^2$$

Graph it.



Find the center and radius.

$$(x - h)^2 + (y - k)^2 = r^2$$

$$1. \ x^2 + y^2 - 16 = 0$$

$$x^2 + y^2 = 16$$

$$r = 4 \quad C(0, 0)$$

Find the center and radius.

$$2. \ x^2 + y^2 + 8y = 0$$

$$x^2 + y^2 + 8y + 16 = 0 + 16$$

$$x^2 + (y + 4)^2 = 16$$

$$r = 4 \quad C(0, -4)$$

Find the center and radius.

$$3. \ x^2 + y^2 - 4x + 2y - 4 = 0$$

$$x^2 - 4x + 4 + y^2 + 2y + 1 = 4 + 4 + 1$$

$$(x - 2)^2 + (y + 1)^2 = 9$$

$$C(2, -1)$$

$$r = 3$$

Find the center and radius.

4. $x^2 + y^2 + 3x + 4y = 0$

$$x^2 + 3x + \frac{9}{4} + y^2 + 4y + 4 = 0$$

$$\left(x + \frac{3}{2}\right)^2 + (y + 2)^2 = \frac{25}{4}$$

$r = \frac{5}{2}$ $C\left(-\frac{3}{2}, -2\right)$

General Form

$$x^2 + y^2 + ax + by + c = 0$$

$a, b, c \in \text{Real}$

Find the equation a circle with $C(2, -1)$ that goes through $(5, 3)$

$$r^2 = (x-h)^2 + (y-k)^2$$

$$r^2 = (x-2)^2 + (y+1)^2$$

Plug in 5, 3

$$r^2 = (5-2)^2 + (3+1)^2$$

$$r^2 = 9 + 16$$

$$r^2 = 25$$

$$25 = (x-2)^2 + (y+1)^2$$

Find the equation a circle with $C(4, 3)$ that goes through $(8, 12)$

$$97 = (x-4)^2 + (y-3)^2$$

Find the equation a circle with diameter endpoints $(-5, -1)$ and $(-1, -1)$

$$M\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$$

$$M\left(\frac{-5+(-1)}{2}, \frac{-1+(-1)}{2}\right)$$

Center $(-3, -1)$

$$(x+3)^2 + (y+1)^2 = r^2$$

$$4 = r^2$$

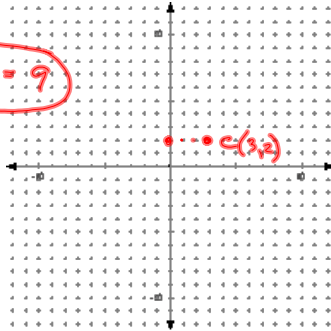
$$(x+3)^2 + (y+1)^2 = 4$$

Find the equation a circle with diameter endpoints $(3, -4)$ and $(7, 2)$

Find the equation a circle, whose center is in quadrant I, with a radius of 3 and is tangent to the y-axis at (0, 2).

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$$(x-3)^2 + (y-2)^2 = 9$$



HW

~~p429-430~~

~~16, 17, 19-21, 24, 27, 33, 34, 39, 43, 47~~

Block day double lesson--Class WORK

p429-430

#s 16, 20, 24, 33, 39, and 43

(do not graph 39 and 43)